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### Class:10+2

Unit: IV

Topic: Electromagnetic Induction & Alternating Currents

### <u>SYLLABUS</u>: UNIT-IV-B

Electromagnetic induction; Faraday's law, induced emf and current; Lenz's Law; Eddy currents, Self and mutual inductance.

Need for displacement current.

Alternating current, peak and rms value of alternating current/voltage; reactance and impedance; LC oscillations (Qualitative treatment only), LCR series circuit, resonance; power in AC circuits, wattles current.

AC generator and transformer.



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- Q.1. Derive an expression for *"Average value"* of alternating current (sine wave)
  - a) Half wave
  - b) Full wave.









- Average value of current is defined on the basis of "Charge" flowing in a circuit.
- Average flowing value of current in a circuit is that a.c which when flowing in a circuit allow same charge to flow as is flowing in a.c. current.ω

b) Full wave: 
$$I_{avg}$$
.  $T_{avg}$   $T_{avg}$ 

$$i$$
  
 $i = l_m \sin wt$ 

t -

$$= \int_{0}^{T} I_{m} \operatorname{sinwt} dt = 0. \operatorname{so}, \qquad \qquad \boxed{I_{avg} = 0}$$

- Q2. Derive an expression for *"RMS"* value of alternating current (sine wave)
  - a) Half wave
  - b) Full wave.

Ans.

• RMS value is defined on the basis of "Heating effect".

RMS value is that *dc* current which when flowing in a resistance gives same heating effect as given by alternating current.



FORM FACTOR:



(Ratio of r.m.s value to avg. value)

$$= \frac{\frac{I_{max}}{\sqrt{2}}}{\frac{2}{\pi}I_{max}}$$
$$= \frac{\pi}{2.\sqrt{2}}$$
$$= 1.11$$



Fig. IV (Phasor diagram)

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## Q3. Find magnitude and phase of current in pure resistive (R) circuit when sine voltage is applied across it?

Q4. Find magnitude and phase of current in pure induction (L) circuit when sine voltage is applied across it.



### <u>Step 2</u>:-

Write relationship between *i* and v



Integrating both sides

$$\int di = \int \left(\frac{V_m}{L}\sin\omega t\right) dt$$

$$i = \frac{V_m}{L} \left(-\frac{\cos wt}{w}\right)$$

$$i = \frac{V_m}{L\omega} \left[\sin\left(wt - \frac{\pi}{2}\right)\right]$$

$$i = I_{max}\sin\left(wt - \frac{\pi}{2}\right)$$

$$\begin{cases} \text{where } I_{max} = \frac{V_m}{L\omega} = \frac{V_m}{X_L} \text{ Inductive reactance} \end{cases}$$



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<u>Step 3</u>:-

Phasor diagram

Current lags voltage by  $\frac{\pi}{2}$ 

### Q5. Find magnitude and phase of current in pure capacitor circuit when sine voltage is applied across it.

### Ans.

### <u>Step 1</u>:-

Draw 2 figures i.e. (Fig. I, II)

v

$$= V_m \sin \omega t$$

The above voltage is applied across a capacitor.





 $v = V_m \sin \omega t$ 

Step 2:-

Write relationship between *i* and *v* 





# Q6. Find magnitude and phase of current in R-L series circuit when sine voltage is applied across it.

Fig.I

Ans. <u>Step 1</u>:-

Draw circuit diagram



### <u>Step 2</u>:-

Mark voltages, currents in circuit diagram.

#### <u>Step 3</u>:-

Draw phasor diagram for voltages



### <u>Step 4</u>:-

Draw Impedance triangle

Fig. III





 $=\sqrt{R^2+X_L^2}$ 

<u>Step 5</u>:-

Draw voltage and current wave form

Current lags voltage by  $\Phi$ 





Discussion for Q.6

1. If L = 0, Z = 
$$\sqrt{R^2 + (LW)^2}$$
  
=  $\sqrt{R^2 + 0}$   
=  $\sqrt{R^2}$   
Z = R

Pure resistive network

 $\overline{V}$  and  $\overline{I}$  are in phase

2. If 
$$R = 0$$
,  $Z = \sqrt{R^2 + (L\omega)^2}$   
 $= \sqrt{0 + (L\omega)^2}$   
 $\overline{Z} = L\omega$   
 $Z = X_L \quad [X_L = L\omega]$ 

Pure inductive network

$$\Phi = 90^{0}$$

Current lags voltage by  $\frac{\pi}{2}$ .

# Q7. Find magnitude and phase of current in R-C series circuit when sine voltage is applied across it.

Fig.I

Ans. <u>Step 1</u>:-Draw circuit diagram



Fig. IV

Fig.II

#### <u>Step 2</u>:-

Mark voltages, currents in circuit diagram.

#### <u>Step 3</u>:-

Draw phasor diagram for voltages



#### <u>Step 4</u>:-

Draw Impedance triangle



Impedance, 
$$Z = \sqrt{R^2 + X_c^2}$$

<u>Step 5</u>:-

Draw voltage and current wave form

Current leads voltage by  $\Phi$ 



#### Q8. Find magnitude and phase of current in R-L-C series circuit when sine voltage is applied across it.



#### <u>Step 2</u>:-

Mark voltages, currents in circuit diagram.

#### <u>Step 3</u>:-

Draw phasor diagram for voltages

$$\overline{V} = \overline{V}_R + \overline{V}_C + \overline{V}_L$$

Inductive effect is more than capacitive effect. (Assumption)

#### <u>Step 4</u>:-

Draw Impedance triangle



Impedance, Z = 
$$\sqrt{R^2 + (X_L - X_C)^2}$$

#### <u>Step 5</u>:-

Draw voltage and current wave form

I 
$$=\frac{V}{Z}$$

Current lags voltage by  $\Phi$ 









# Q9. What is "Resonance" in R-L-C circuit? Derive expression for resonant frequency?

#### Ans.

a) Resonance in R-L-C circuit means condition when current is optimum.
 That is for series R-L-C circuit, current is maximum.

b-1) As 
$$\omega$$
 changes,  $X_L = L\omega$  and  $X_C = \frac{1}{C\omega}$  change



current is maximum.

b-3) Three station frequency is fed in transistor circuit. Sharpness of resonance curve should be high



 $I_2$  and  $I_3$  are currents due to station 2 and 3 when station 1 is tuned at frequency  $f_1$ 



 $\omega \rightarrow variable$ 





- Q10. a) Prove Energy stored in an inductor is  $\frac{1}{2}$ . *L*.  $I^2$ ? b) Prove Energy density in magnetic field is  $\frac{1}{2}$ .  $\mu$ .  $H^2$ ?
- Ans.a) Energy is stored in an inductor in form of magnetic field.

When current increases from *I* to I + dI, flux linking increase.

Rate of change of flux causes an emf *e* as shown in diagram.

= e dq

= e Idt

 $= \int e I dt$ 

Battery does work against e and energy supplied by battery gets stored in inductor in form of magnetic field.







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w

$$= \int L \frac{dI}{d\ell} \text{ I. } d\ell$$
$$= L \int I dI$$
$$= L \left| \frac{I^2}{2} \right|_0^{I_0}$$

Energy stored 
$$=\frac{L}{2}I_0^2$$

Energy stored 
$$=\frac{1}{2}LI_0^2$$

b) Energy Density:

Energy Density  

$$= \frac{Energy}{Volume}$$

$$= \frac{1}{2} \cdot \frac{L \cdot l^{2}}{A \cdot l}$$

$$= \frac{1}{2} \cdot \frac{\frac{N^{2}}{R_{e}} \cdot l^{2}}{A \cdot l}$$

$$= \frac{1}{2} \cdot \frac{N^{2}}{R_{e}} \cdot \frac{l^{2}}{A \cdot l}$$

$$= \frac{1}{2} \cdot \frac{N^{2}}{R_{e}} \cdot \frac{l^{2}}{A \cdot l}$$

$$= \frac{1}{2} \cdot \frac{N^{2}}{\frac{l}{\mu \cdot A}} \cdot \frac{l^{2}}{A \cdot l}$$

$$= \frac{1}{2} \cdot \mu \cdot \left(\frac{N \cdot l}{l}\right)^{2}$$
Energy Density  

$$= \frac{1}{2} \cdot \mu \cdot H^{2}$$

$$OR$$

$$= \frac{1}{2} \cdot \frac{B^{2}}{\mu}$$

Q11. Find Power associated with a "Resistor" in a.c. ?



Problem:A voltage of 220 volt (A.C) is applied across a<br/>resister of value 100Ω. Find reading of watt<br/>meter connected in the circuit.

Q12. Find Power associated with an "Inductor" in a.c.?





Problem:A voltage of 220 volt (A.C) is applied across a<br/>capacitor of value  $12\mu F$ . Find reading of watt<br/>meter connected in the circuit.

## Q14. Prove P = $V_{rms} I_{rms} \cos \phi$ , where $\phi$ is phase difference between voltage and current?



Therefore, current through pure *L* or pure *C*, which consumes no power for its maintenance in the circuit is called idle current or wattles current.

### Q15. What is an L-C oscillator? Derive expression for resonant frequency of L-C oscillator?

Ans. L-C Oscillator is a parallel combination of *L* and *C* as shown in the Fig. Energy is stored in *L* in form of magnetic field. Energy is stored in *C* in form of Electric Field. Energy keeps on oscillating from magnetic to electric and vice versa. Under resonant conditions I is zero and  $|\overline{I}_L| = |\overline{I}_C|$ .

When 
$$|\overline{I}_L|$$
 =  $|\overline{I}_C|$   
 $\overline{I}$  =  $\overline{I}_L + \overline{I}_C$   
= 0  
 $\overline{I}$  =  $\overline{I}_L + \overline{I}_C$   
 $|I_L|$  =  $|I_C|$   
 $X_L$  =  $X_C$   
 $L\omega$  =  $\frac{1}{L\omega}$   
 $\omega^2$  =  $\frac{1}{LC}$   
 $\omega$  =  $\frac{1}{\sqrt{LC}}$   
 $2\pi f$  =  $\frac{1}{\sqrt{LC}}$ 



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#### Q16. What do you mean by Quantity factor of a circuit? Explain.

Ans. The characteristic of series resonant circuit is determined by the Q factor or quality factor of the circuit. It defines the sharpness of tuning at resonance.

Q 
$$= \frac{voltage \, across \, L \, or \, C}{applied \, voltage \, (voltage \, across \, R)}$$
Q 
$$= \frac{1}{R} \sqrt{\frac{L}{C}}$$

The difference  $w_2 - w_1 = 2\Delta w$  is called the band width of the circuit. It defines sharpness of tuning at resonance.

The values of *Q* usually vary from 10 to 100.

#### **Q17**. Discuss Construction, Working and Efficiency of a transformer.

Ans. Transformer is a device used to change A.c. voltage level/current.

Core is made up of soft iron laminations.

= 1000 or more  $\mu_r$ 

Core is in form of laminations to decrease eddy current losses/heating. Input is given to primary winding. Load is connected across secondary winding.

Number of turns of primary  $(N_1)$  can be less than, equal to, greater than number of turns of secondary  $(N_2)$ .

Thickness of wires depends on current to be carried Primary and Secondary are co-axial for practical purpose, i.e. flux linking is max.

#### Working

(i) 
$$\frac{emf}{turn} = \frac{d(flux)}{dt}$$
 is same for all turns.



Core diagram

Law of conservation of energy (Assumption): No (2) losses in transformer

Input Energy = Output Energy

$$V_{1}. I_{1} = V_{2}. I_{2}$$

$$\boxed{\frac{V_{1}}{V_{2}} = \frac{I_{2}}{I_{1}}}$$
(2)

From (1) and (2)

$$\frac{V_1}{V_2} = \frac{N_1}{N_2} = \frac{I_2}{I_1}$$

(3) Efficiency, 
$$\eta = \frac{output}{input} = \frac{V_2.I_2}{V_1.I_1}$$



Primary wiring

(Output = Input - Losses)



